Subject: T.O.C



Your Personal Exams Guide

			You	r Personal Exams Guide
Serial Number	Date	Title	Page Number	Teacher's Sign/Remarks
1.		· Introduction of T.O.C. D		
2.		* Regular expression and finite Automata. 2		
36		Regular language and Context free language. 2		
4.		· Context free grammax and  Push down automata.	ige .	
5.		• Turing Machine.		<i>)</i>
5.		· Closure properaties of language.		N :
7.		· Uniountability.		
2.		· undecidability · (4)		
8.		· pumping lemma. 2		
			•	



## INTRODUCTION OF TOC

	THE NO DOCTION OF TOL
	No V prime and the last of the
	Automata :- Study of abstruct computing devices or machines.
	Symbol - A symbol is an abstruct entity.  Example: a,b, o,1,
	Alphabet: An Alphabet is a finite collection of Symbols.  (E) example: S = {a,b,c}
	$\Sigma = \{0, 1\}$
•	String: It is a sequence of Symbols.  Example: \( \Sigma = \{\( a,b\} \)
e +4	strings: - { a, b, aa, ab, ba, bb} herre have 6 string.
1	> tmphy string can be denoted by (for 1 or 1).  [If the length of string is Zerro, Such string is called
	empty string
	Language: - collection of string.
Sati	→ Σ = {a,b}
	= \{aa, ab; ba, bb \}
2	Where language 11 is finit language.
- A	$\rightarrow \Sigma = \{a, b\}$
	= Sa, aa, ab, aaa, aab, aba,? 'a'.
	where 12 is infinit language.
	Length of string: No of symbols contained in a string.
	{ab2 => length 2' · 1∈1 => length o'.



	Your Personal Exams Guide		
	Prefix of a String: - If W = XY, Pore some string y, then		
11.11	vis a preafix of w		
	• •		
	$= \frac{1}{2} \frac{1}{2} = \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} = \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} = \frac{1}{2} \frac{1}{2$		
	$= \frac{20011}{x} = \frac{20011}{x} $		
	Suffix of a string: - If W = XY, fore some string X, then y is		
	a suffix of w.		
3	example - W= 300113		
	$= \underbrace{\{001(1)\}}_{X} = \underbrace{\{1,11,011\}}_{Sullix}$		
	x y suffix.		
	CKKleen closurce:		
	Control of the second of the s		
	-> It is denoted by * Casterisk) after the name of the alphabet.		
	is 5th. This notation also known as the Kleene State.		
the same	The second secon		
	$1f \Sigma = \{a, b\}$		
	Σ = set of ay strings of length o', = ξ ξ ?.		
	Σ'= set of au strings of length 1 = {a, b}		
· · · · · · · · · · · · · · · · ·	$\Sigma^2 = \Sigma \cdot \Sigma = \{a,b\} \{a,b\}$		
	= {aa, ab, ba, bb} = set of all strings of lengthis.		
	5-555-		
	Σ³= Σ Σ Ξ = set of all strings of length '3'.		
	[\Si^3 = 8 (no of straing)		
	151-29		
	IZI = 22 = set of all strings of length in.		
a Aus	$\Sigma^* = \Sigma^0 U \Sigma^1 U \Sigma^2 U \cdots$		
	= {E} U {a,b} U {aa,ab,ba,bb} U		
i i	Z = solob mil vining soulling solom Sm 12 [1]		
	$\Sigma^{+}=$ set of all string possible over $\{a,b\}$ Luniversal set $\Sigma^{+}=\Sigma^{+}\cup\{E\}$ .		
	[2-2-07-5]		



	Your Personal Exams Guide			
	$\sum_{i=1}^{\infty} \frac{1_{1} \cdot 1_{2}}{1_{3}} \qquad \frac{1_{1} \subseteq \Sigma^{*}}{1_{2} \subseteq \Sigma^{*}}$			
	$\begin{array}{c c} & & & & \\ \hline \end{array}$			
	→ no of string possible over ∑* is infinite.  → no of Language possible over ∑* is infinite.			
	1_ Clanguage) -> A program is a string.			
. V .	(String) S -> FA > Yes.  Set of all valid program.			
	1 = set of all strings which starts with a.			
	Initial  State (A)  B)  Final State.			
	(e) park			
	String = aab (present In Language or not)  this string are accepted by FA. A > B > B B B			
	The string will be accepted by FA, If after scaning entire string we reach in final state from mitual state.			
	this straing are not accepted by FA. A by (b) (a) c			
	positive closure:  The 't' (plus operation) is some times called possitive			
	elocure. $\rightarrow 1f = \frac{2}{3}a, b\frac{2}{3}$ , then,			
	$\Sigma^{+} = \{ a, aa, ab, ba, bb, \cdots \}$ $\Sigma^{+} = \Sigma^{*} - \{ \epsilon \}$			
	Scanned by CamScanner			

	Your Personal Exams Guide
	Substruing of a string:
	->Astring 'w' = abc
	here, ab, bc are substring of of other w.
	But ac are not substring of w.
•	Concatenation of two string:
_/	<u> </u>
1.11.1.1.1	-> If x, y \in Z *, then x concate nated with y is the world
9	formed by the symbol of X' followed by the symbols of Y.
<b>J</b>	This is denoted by x.y. It is same as xy.
	A STATE OF THE STA
e	Reversal of a string:
- /	
	-> Criven a straing Wilt reenersal denoted by WR is the
	oriven a straing w, it reversal denoted by whis the straing spelled back wards.
	w = ab
	$W^R = ba$ .
6	Gercamman:
	-> It enumercates string of the language.
	> It is a finite set of rules defining a language.
	> A grammare is defined as 4-tuples (V,T,P,S)
	Where Ty -of non terminals.
) - 2 PL 12 - 1	T(E) -> Set of Input terminals.
fortal de	P Finite set of production teule.
	(3 > Start of cymbol.
	> Start(s).
	example: $S \rightarrow aSB$ here, $v = \{S, B\}$
	$(production)P = S \rightarrow AB \qquad T = \{a, b\}$
	$(production)P = \begin{cases} S \rightarrow AB \\ B \rightarrow B \end{cases}$ $T = \{a, b\}$
	-> Gretting a strong from a grammate is called percivation.
-	



	Tough Growing Examine Salad
	Deningham
	Denivation on aabb
	$s \rightarrow asb$
	> aaBB [s > aB] (> entire process called derivation.
7	-> aabB [B -> b] sequential forms.
	→ Jaabb [B → b]
	JULIAD [15-7b]
	8-1)
	constitute a greammak given the fallowing language,
- 10	1 = 3 Setuation length 2 4
3 49	$\Sigma = \{a, b\}$
	$1 = \{aa, ab, ba, bb\} $ $(a+b) (a+b)$ $A$
- 44	
•	S -> aa/ab/ba/bb. >> production nules.
	$S \rightarrow AA$
1 1	$A \rightarrow \alpha/b$
	A
- 12	
0	03-2 Construct grammar, given the following languag,
293	$1 = \left\{ a^{m} / m > 0 \right\}$
	> 1= \( \xi \alpha  \alp
	P·R→
	$1 \int 3 \rightarrow 95/\epsilon$
. 6	$S \rightarrow Sa/F$
1 12/1	
2 (6)	
500	(5 /2)
	7 / 2
4.08	€ /
100	(D-3) construct grammat, to generate (a+b) .
7	
13	$\rightarrow  s \rightarrow as/bs/e $ (a) (a)
W. 77	(b, s)
10 pt on the	$(\epsilon)$



	Your Personal Exams Guide
	[0-4] construct a grammare, given the following language,
	1 = { set of all chaing of length atteast 2? }
24.0	$\rightarrow L = \{aa, ab, ba, bb, aaa, aab \dots \}$
	(a+b) (a+b) (a+b)*
	production teules,
- 187 - 18	$S \rightarrow AAB$
	$A \rightarrow \alpha/b$ .
	$B \rightarrow \alpha B/bB1\epsilon$
	To El a A A To A so Alea Palla sina lamana de m
	1= \( \frac{1}{2} \) string of length at most 2' \( \frac{1}{2} \).
	2719 (2719)
	$\rightarrow \perp = \{\epsilon, \alpha, b, \alpha\alpha, \alpha b, b\alpha, bb\}$
	(a+b+E) (a+bE)
	production rules;
y =	
	$S \rightarrow AA$ $A \rightarrow 0/b/\epsilon$
6	(8-6) 1 = { start with a and end with b 3.
	$\rightarrow$ here $\alpha (\alpha + b)^{\dagger} b$
	production rules,
	proceeding
	$S \rightarrow a A b$ (abb)
	$A \rightarrow aA/bA/E$ $gA$
	- C set of
	05-7) 1= 3 all string starting and ending with different
	cymbol ?
	$\rightarrow a(a+b)^*b + b(a+b)^*A$
	PR:- S-> aAb/bAa.
	$A \rightarrow \alpha A/bA/E$



	rour craonar Exama Odiac
	10-8 1= { Set of all straing, and ending with same symbol?
- 1	$\rightarrow \alpha (a+b)^*a + b (a+b)^*b$ .
	$S \rightarrow aAa/bAb/b/a/E$
	$A \rightarrow aA/bA/e$
	$[8-9]$ construct a grammar, given the following language. $L = \{a^m b^m / n > 1 \}$
	$\rightarrow L = \{a^{m}b^{m}/m\}/1\}$
	= \{ab, aabb,}
	$s \rightarrow asb/ab/\epsilon$ s, s
	(9,5-b) - (9 5-b)
	65-65
- 1	aabb
5-3 A	[B-10] constitut greammates that aaabbb
	(B-10) constituet greammation that aaabbb generate set of all palindrom -
	WWR, WaWR, WbWR
	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	$\rightarrow S \rightarrow aSB/bSb/a/b/e$ a ja $a \rightarrow a$
1 100	and
	[05-11] construct grammate that genetrate even length
	01.2.00%
	$\rightarrow 1 = \{ aa, ab, ba, bb, aaaa, \dots \}$
<u> </u>	((a+b)(a+b))*
	$\begin{array}{c} S \rightarrow BS/\epsilon \\ Q \rightarrow AA \end{array}$
	$A \rightarrow 0/b$



	Your Personal Exams Guide
	$[8-12] 1 = \{a^{m}b^{m}/m, m > 1\}$
	$\rightarrow 1 = \{ab, aab, aab, abb, \dots \}$
	1= 300,000,000,000,3
	3 M. and water
	$S \rightarrow AB$
	$A \rightarrow A / A \rightarrow A^{m}$
-14	$B \rightarrow bB/b \rightarrow a^m$
•	$[0,-13]$ $1 = \{a^m b^m c^m / n, m \geq 1\}$
	S
	$\rightarrow$ $S \rightarrow AB$
	$A \rightarrow aAb/ab$ $(a \rightarrow b)(c)$ $(a \rightarrow b)(c)$ $(a \rightarrow b)(c)$ $(a \rightarrow b)(c)$
	$B \rightarrow cB/c$ (ab) (gB
3/	aabbccc
<u>U</u>	$\Delta = \{a^{m}c^{m}b^{m}/m, m \neq 1\}$
d.	> S > a S b / a A b }
	$A \rightarrow cA/c$
2	$\begin{pmatrix} 1 \\ e \end{pmatrix}$
	Smmm, m / aacbb
	[0-12] T= {0, 2, 2, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3,
1.42.11	$\rightarrow$ $S \rightarrow AB$
	$A \rightarrow aAb/ab \Rightarrow a^n b^n$
	B -> e.Ba/ca -> cmdm
	$\frac{100-16}{100} = \frac{200}{100} = \frac{200}{100} = \frac{200}{100} = \frac{100}{100} = \frac{100}$
-	$[0,-16]$ $1=\{a''b'', a''b''\}$
	$\rightarrow (8 \rightarrow a8bb/abb)$



05-17 L={am+n bm cn/m,n),1} { m m m m m m / m, n), 1} S-) a Sc/a a Ac. aabbcccc=> a2 b2 (2+2) => 02 62 64

Scanned by CamScanner



	Comsky Hierachy: Comsky hie teachy consists of	
- 1/	following four types of classas	
	(generalors) ranguage (REL)  Grandine  (acceptor)	_
	Wild /	•
	Sensitive	
	(CSL) Type-21 LBA	
	1715 3	
	Context free push down automata	
	(PDA)	
	Type-3)	
	regular finite state	
	language Automata	
	(RL) (FA)	-
		1
		•
	(Chomsky, Hiercatechy),	
/6	Types of Geteammeres:	
	1) TYPE-O GIRAMMAK (Unitertricted Girammare):	,E
	C) T/T O STICKMAN CO	
	-> These are unrestricted grammate which metude	
	·	
	all foreman language.	152
	-> This grammate generale exactly all language that	,
	Can be trecognized by a tutting machine.	
	A \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	
	-> Rules are of the form d > B	
	(a must have at least 1 Non-	
	terminal.)	
	-> where &d and B are architrary sequence of	
	terminals and non-terminals and dff.	
	$ex - \sqrt{A \rightarrow aA \mid bA \mid} \mid^{X} a \rightarrow B a \mid$	



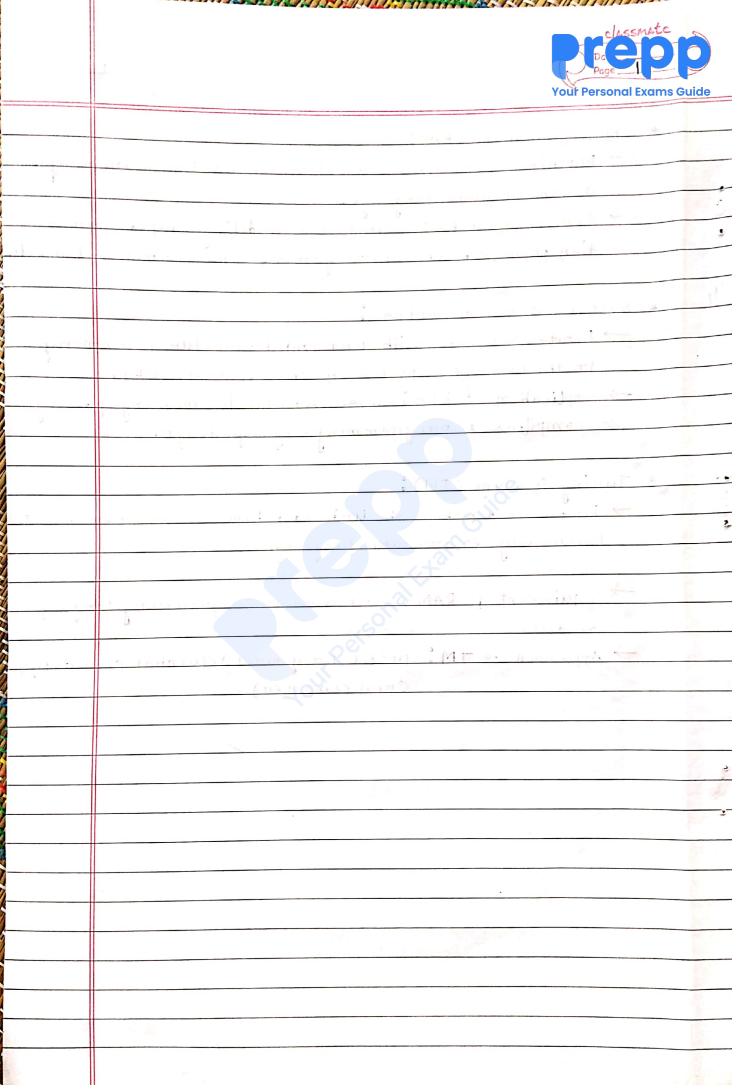
Your Personal Exams Guide
2) TYPE-1 GIRammars Context Sensitive GIRAMMAR):
> language defined by type-I grammares are accepted by the linear bounded automata.
> Rules are of the form, Id1 XIB1  Length of d'is less than or equal to rength of B'.
A>E is not allowed unless A is a start symbol.  X AB > a, VIA > aB,  3 Type-2 Gerammare (context sensitive Greamman)
→ Language defined by type-2 grammare are anepted  by push down automata.  → Rules are of the form d→β.  Where, & d = single nonterminal.
A) Type-3 Girammare (Regulair Girammare)
→ language define by type-3 grammatis are auepted  by finite State automata.  → Regulare grammate cun follow either right
Linear are left linear $\frac{1}{A}$ (right linear grammate) example, $\frac{A \to \alpha B}{B} = \frac{A \to \alpha B}{A \to \alpha B}$ $A \to \frac{B}{B} = \frac{B}{A \to \alpha B} = \frac{B}{A$
ABEY  (Jerminal)  ABEY  (Jerminal)  ABEY  (Jerminal)  ABEY
If, $[A \rightarrow Ba/a] \rightarrow not$ Type 3 gramma.

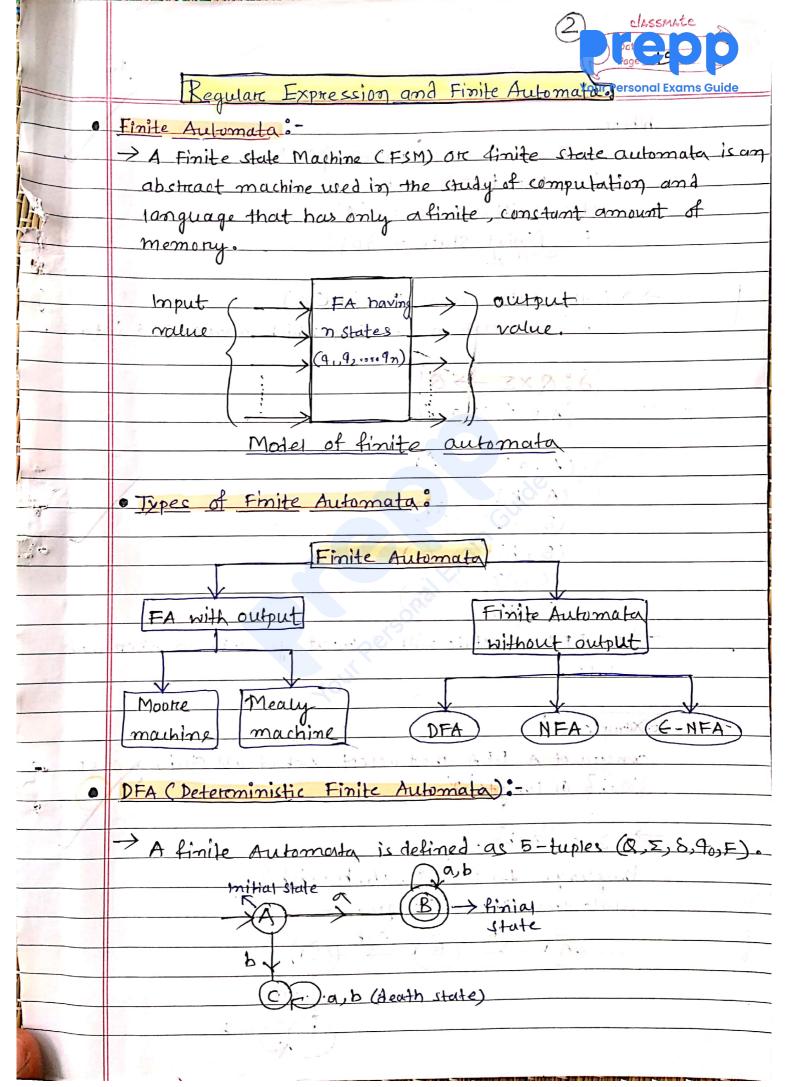
Scanned by CamScanner

	Your Personal Exams	Guide
	· Chomsky hireartchy Examples-	
	· Identily grammare:	
	1) Example 1 2) Example	
	S -> aSb aA B S-> a aA Bb	
	$B \rightarrow \alpha A / \alpha$	-
	$C_{c} \rightarrow cDDD$ $\rightarrow (Type-2)$ .	<u> </u>
	It will be accepted by	
j.	-> ans is (Type-0) Push Down automata	,
	it will be accepted by	•
	Turing machine.	
	Lite personne saddi in properti in a company in a company in the c	
	3) Example-	
	to be a second to the second t	
	S-> asb ab -> (Type-2) grammar.	1
	/ Jest por John Son John St.	
	Type-oxides is also called as:	
		-
	-> Unicestracted Greammaix.	
	-> Recursively Enumericable languages.	7
	-> Turing Machine.	***
	Type-1 class is also called as:	
	-> Context Sensitive grammati.	
	-> Context sentisitive language.	2 - 20
	-> Linear Bounded Automata.	3
		禁止
	Type-2 class is also called as:	
11 14 d	-> Context Free Circamman.	5
	-> context tree language.	-25
	-> push down automata.	
	Type-3 dass is also ealled as:	
d/3	The same of the sa	
	-> Regulate language, -> finit automata.	
	→ finit automata.	The said



	Popul
3	Your Personal Exams Guide
	Finite Automata (FA):
	-> Machines with fixed amount of unstructured memory,
<u></u>	telepts regular language.
<b>3</b>	Application of FA: weful for modeling chips, communica-
3	-> Application of FA: useful for modeling chips, communica- tion protocols, adventure games, some control cystem gets.
Z V	Push lown Automata (PDA):
	-> Finite Automata with undounded structured memory
2	In the form of a push down stack, accepts CFI.
	-> Application of PDA: Compiler useful for modeling parsing,
	Compilens » programming language design.
-	Turing Machine (TM):
* 1	> Finite automata with undounded tape accepts on enumerates
	Recursively enumerable language.
	-> Equivalent to RAM's and various programming language
	-> Application of TM: Model for general Sequential computation
	Ctrean computer).
	40
4	
9	
1.53	
37	



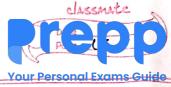




	Your Personal Exams Guide
	Where,
1	a = set of all states => {A,B,C}
-	$\Sigma =  mput = \rangle \{a, b\}$
	90= Initial State => 'A'.
	F=finial State => {B}
	· · · · · · · · · · · · · · · · · · ·
	→ a is the supercret of F. (FCQ)
	S= treansation function which maps QXE into Q.
	S:QXE -> Q
	ξΑ,Β, c <sup>2</sup> χ ξα, b <sup>2</sup>
	A Same as the same and the same
	$(A, \alpha)$ $(A)$
	(A, b)
	(B, 9)
	(B, b)
	(C, b)
	-> im DFA a state with 1 Imput go Into another one
_	.ctate.
	A TONE OF THE PARTY OF THE PART
	Example-1
	Construct A DFA that accept set of an string over ? {a,b} of length 2'.
	Earby of length 2 will have bining the
_	> - Sa h?
	$\Rightarrow \Sigma = \{a,b\},$
_	language, == {aa, ab, ba, bb}.
	State transation Diagram -
	A $B$ $A$ $B$
	alice diservais
	(P) a,b
_	

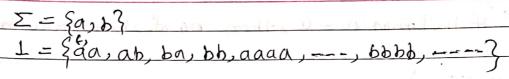


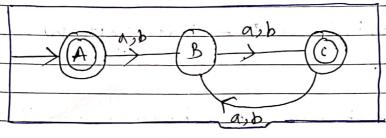
	Your Personal Exams Guide
	String accept -> Scan the entire string, if we reach ina finial state from initial state. Then string will be accepted by FA.
	a language if all the string in the language are accepted and the string in the language are rejected.
	Construct a DFA which accepts all the String {a,b} where the string length is accept 2?. IWI > 2
	$\rightarrow A$
	State transation Diagram,
1	Construct a DFA, OBS = {a,b}, W = {a,b}, 121 52.
2	$\Sigma = \{a, b\}$ $L = \{E, a, b, aa, ab, ba, bb\}$ Stata transation Diagram,
	a,b a,b A B A C A A B A A B A A B A A B A A B A A B A B A B A B A B A B A B A B A B A B A B A B A B A B B A B B A B



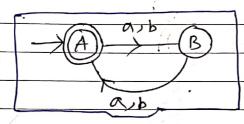
	Your Personal Exams Guige	_
	( X-14) W> string	
	(#)  w =2,  w /2,  w  <2. (gate)	
)		
	-> with an estraine lemeth 1/2/1= m, then	No.
	-> when, String length [w] = n, then no for State trequired (n+2).	-
	when, (w) >m, them	
	no of state required (n+1).	14
	110 03 04/10 124	
	When, Iwl (n) then	
, ,	no of state required (n+2)	
	10 05 37012	
	·1W1=2 · W/2	-
	$L = \{aa, ab, ba, bb\}$ $L = \{aa, ab, aua \cdot \cdot \cdot \}$	-
	-A) B) C -A) B) C a,b	4
	(n+1)	-
	()()	4
	(D)	-
	(nt2) (1-States)	-
	· W1≤2	
	$1 = \{\epsilon, \alpha, b, a\alpha, ab, ba, bb\}$	-
	ab 926	1
٠,	$(A) \rightarrow (B) \rightarrow (C)$	-
	y as b	
	(m) (p) (a, b)	1
	(4-states)	-
	manufic resignment and the	
	Example]-4	
	DEA inhigh deept all straight	
	20/21 Sa b ( 1/4)1 mad 2 = () (m)20/49 1/4	f
	Changen of string will be even)	111
	- Jany Maria	_
$-\parallel$		-







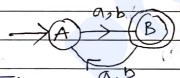
016



(State transation Diagram)

(Ex-5), [12] mod 2 = 1]

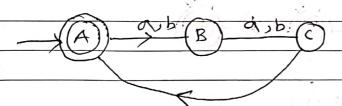
=> 1 = {a,b, aaa, bbb, ...aaaaa, ...}



Ex-6)

[12] mod3=0

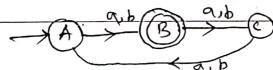
1 = aouo {t, aaa, aba, bbb ....}



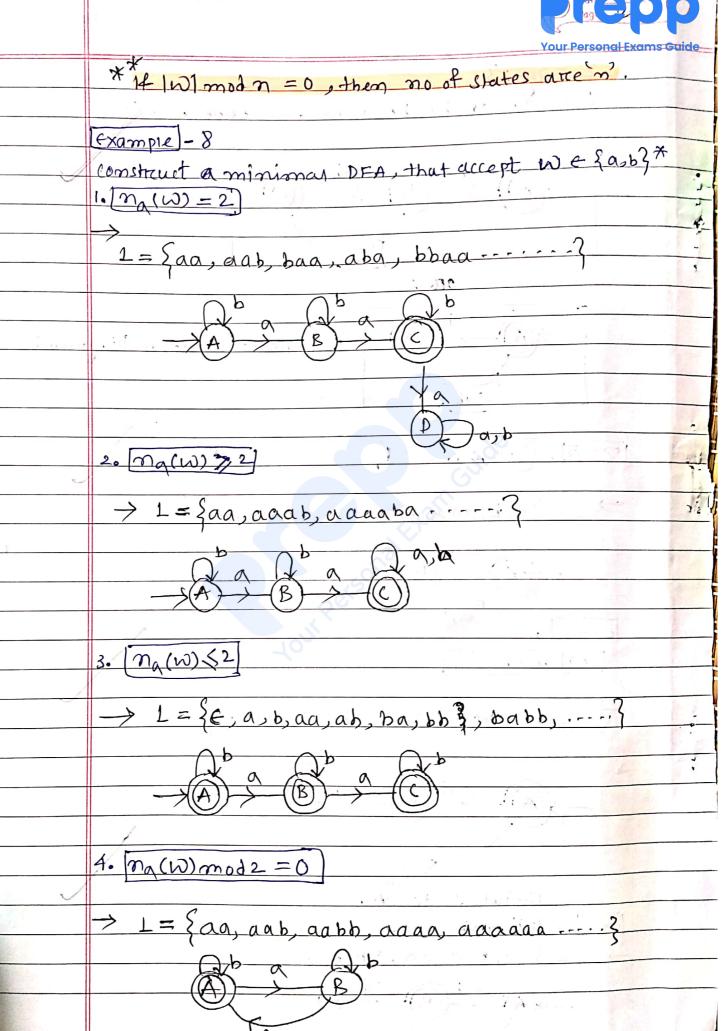
finial State 'A'.

Ex-7, 121 mod 3=01

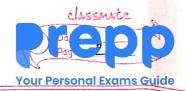
> 1 = { a, b, aaaa, bbbb, ....?







	Your Personal Exams Guide
F	5. Ma(w) mod 3 = 0
	The state of the s
de la company	> 1 = {aaa, aaaaaa }
	State transtation diagram-
1	Qba Qba Qp
A. Carrier	$\begin{array}{c c}  & & & & & & & & & & & & & & & & & & &$
	0 1 2
	6. Construct a minimum DFA, Where W + {a,b}*
	21. w C = (w) co-
-4	$m_{\alpha}(\omega) = 0 \mod 2$
2	$(n_b(\omega) \cong 0 \mod 2)$
. 2	
	-> 1= {e, aa, bb, aabb, abab, bbtaaaa, bbbb}
	Qb Qb. Qa. Qa
A	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
76	
a. 1	# of state {A,B} # of state {C,D}
	IN A MINIO LANCELL
	Cross product method-
2	
17	$\{A,B\}$ $\times$ $\{C \times D\}$ = $\{A(AD,BC,BD\}$
	ee o o o o o
	(AC) (BC) AABA
	A b b b b b b
	(AD) q (BD)
	60
	e ake = {e el (dinian Stale
	e one = {ee, eo, oe? state (finia) state).

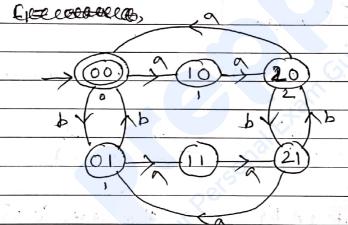


I The Automata contain n' state and the other
automata Contain in number of states then there
Chois product going to contain, (mxn) states.

Denstruit a minimal DFA which accepts set of all strings.

Over {a,b} in which no of a's are divisible by 3 and not of b's are divisible by'2'.

 $\rightarrow \omega \in \{a,b\}^{\uparrow}$   $n_a(\omega) \cong 0 \mod s$  $n_b(\omega) \cong 0 \mod 2$ 



finial state (00)

When, na (w) mod 3 / nb (w) mod 2

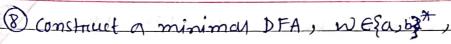
finiar state= { 10, 20, 11, 21}

m

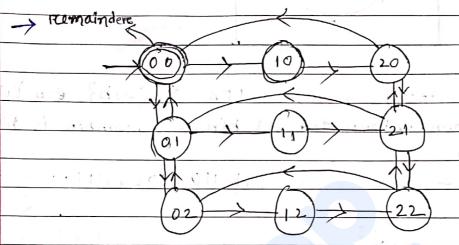
When my (W) mod 3 = n, (W) mod 2

fininal state = {00,113;





 $m_{\alpha}(\omega) \cong 0 \mod 3$   $m_{\beta}(\omega) \cong 0 \mod 3$ 



When, na(w) mod 3 = 1

nb(w) mod 3=2, then

finial state = {1,23

when, na(w) mod 3 > nb(w) mod 3, then

finial state = {10, 20, 21}

Then the minimum no of states in automatais mxn'.

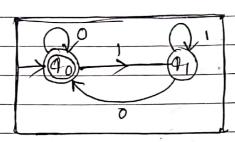
example-9]-D

construct a minimal DFA, which accepts set of all string Over {0,13, which when interpreted as binary

 $7 = \{0,1\}$   $w \in \{0,1\}$ 

If we divided any no by 2 reminder can be o or 12.

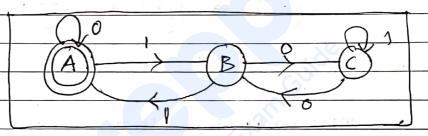
L= \{0,00,000,000,0000, ----, 10, 100, 110, ----}



- Denstruct a minima DFA, Σ=ξα, β, επ ωεξα, β\*

  when interpreted as binary number is divisible by

  3.
- $\rightarrow 1 = \{0, 60, 000...., 11, 110, 1100, 1111......\}$



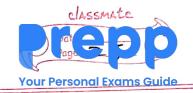
Finite Automata Con represent intro ways

State Diagram transation Diagram.

State transation table.

State transtion table,

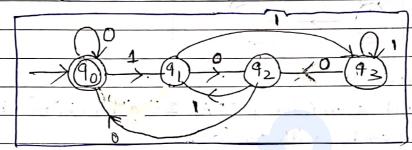
		0 1
	>*A	$A \rightarrow B$
1.	(F) 1.3	- F. 19 11
· · ·	В,	CA
	(	B



3 construct a minimal DFA, which accept all string
Over {0,13 which when Interpreted as a binary
number it divisible by 4.
<b>V</b> ,

$$\rightarrow \Sigma = \{0,1\}, 8W \in \{0,1\}^*$$

L={0,100,000,---,100,1000,1100,1000,10100,---}



State transation table—

The reminder is = 0

Then Fs and then Fs and the reminder is = 1

The reminder is = 2

The reminder is = 2

The reminder is = 3

Example - 10

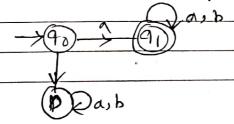
Construct a minimal DFA, Which accepts set of all strings, Over Early? where each String starts with an 'a'.

 $\rightarrow \Sigma = \{a, b\}$ 

W={a, b}\*

language, Li={a, aa, ab, aaa .. }

state transation Diagram,



- then take the smallest string and make its skeleton.

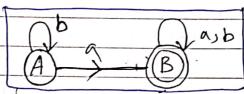


Example-11

Construct min minimal DFA, Z={a,b}, W={a,b}\*\*

"Wheke each String Contains a"."

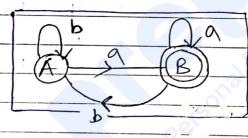
 $\rightarrow \bot = \{a, aa, ab, ba, aaa, \dots \}$ 



[Example-12]

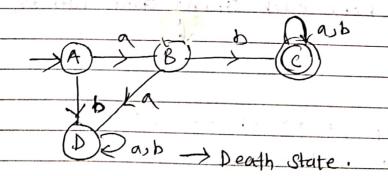
Construit a minimar DFA; I={a,b2, W+{a,b3\*} String ends with an 'a'.

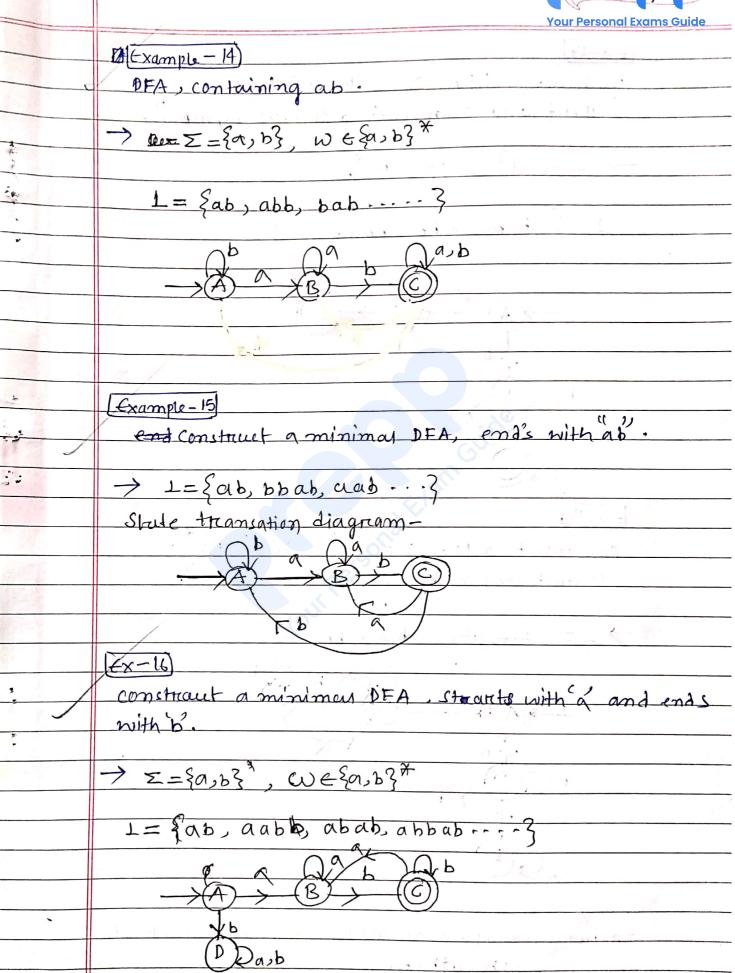
→ L={a, aa, ba, aaa, bba, baa, bbba....}



Example -13

Construct a minimal DFA,  $\Sigma = \{a,b\}$ ,  $W \in \{a,b\}^*$  C each string start with ab". C =  $\{a,b\}$ , A =  $\{$ 







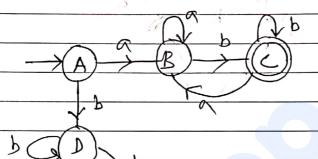
16x-17

Construct a DFA, Z={a,b}, WE{a,b}\*.

U start and ends with different cymbo".

 $\rightarrow \Sigma = \{a,b\}, W \in \{a,b\}^*.$ 

1 = {ab, ba, abb, bba----}

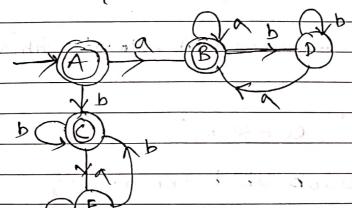


GX-18

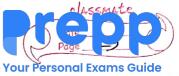
Construct of DFA,  $\Sigma = \{a,b\}$ ,  $w \in \{a,b\}^*$ .

Clistant and ends with same symbol?

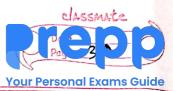
> 1= aaze, a, b, a a, bb ...}



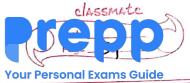
-> here, Example - 17 and 18 are complement of -



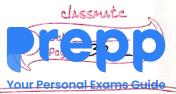
	Your Personal Exams Guide
	(EK/JA)
	> 1 and 12 are 2-language, then 11 is said comprement
	$1 = \Sigma^{+} - 12$
	1/ 1/2 1/3 1/3 1/3 1/3 1/3 1/3 1/3 1/3 1/3 1/3
X	Complementation of DFA:
	1={Starting with 23 12={not starting with a3}
	Qasb on and Qasb
1000	$(A) \xrightarrow{A} (B)$
	<b>↓ b ← &gt; 1</b>
: 2	O a,b
	<del>    = 12</del>
	-> Complimentation methode apply for only DFA not for
	NFA. Will be changed
	-> Every thing has to be Same only sing finial state.
- 4	
	Construct a DFA, WE {a,b}*
	Every a Should be followed by a b'.
1 7	- variage of the control of the cont
	$\rightarrow L = \{ \epsilon, ab, abb, abab, babb, \dots, b, bbb, \dots \}$
	State transation Diagram -
	$\rightarrow (B) \rightarrow (C)$
	Ja
	(D) a, b

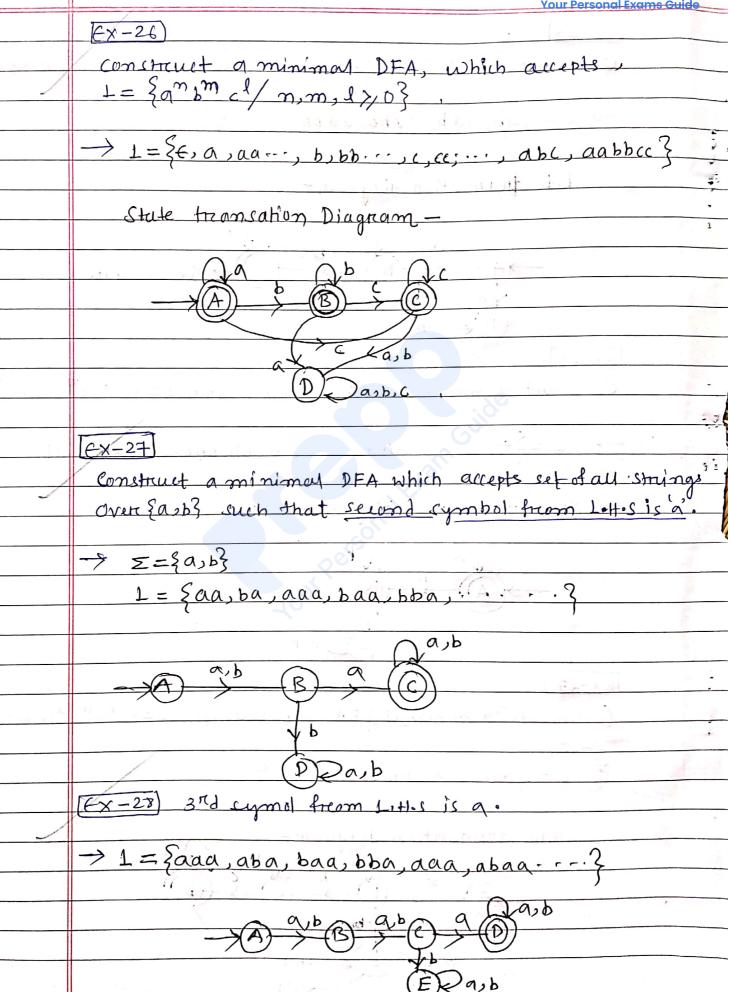


	Your Personal Exams G	uide
	Ex-20	
-	Construct a DFA, Where, WE {a,b} *	200
	Every a'should not never followed by a 'b'.	
	$\rightarrow 1 = \xi \in \{a, b, aaa, ba, aaa, bba, \dots, \}$	. 8
	a in the second of the second	E.
	State transation Diagram -	1
	in the second se	
	Some A Some And A Some	12
	(i) - (i) - (i) - (ii)	
	[EX-2]	
	construct a minimar DFA, where	
r i	$W \in \{a,b\}^{*}$	+7
	every a should be followed by bb	7 %
		3.7
	-> 1= {6,abb,}	
	100	
- 1 to 62 Lu	State transation Diagram-	A COLOR
	R b C	A CONTRACTOR
, "		
		A SE
	(E) a,b	7 34
	finian state = {A,D}, and all ==================================	
	[Ex-22]	2
	Construct a DFA, where.	7
	WE Ea, b3	
-	every 'a' should never be followed by a bb'.	
	every should by a be	1 14
	$\gamma \perp = \{ \epsilon, \alpha, \alpha\alpha, \alpha b, b\alpha, bb, \alpha\alpha\alpha, \dots \}$	8
	a Qua b a b a b cost b clarks	5
	A) B) C) Tenth state.	
	Control of the contro	

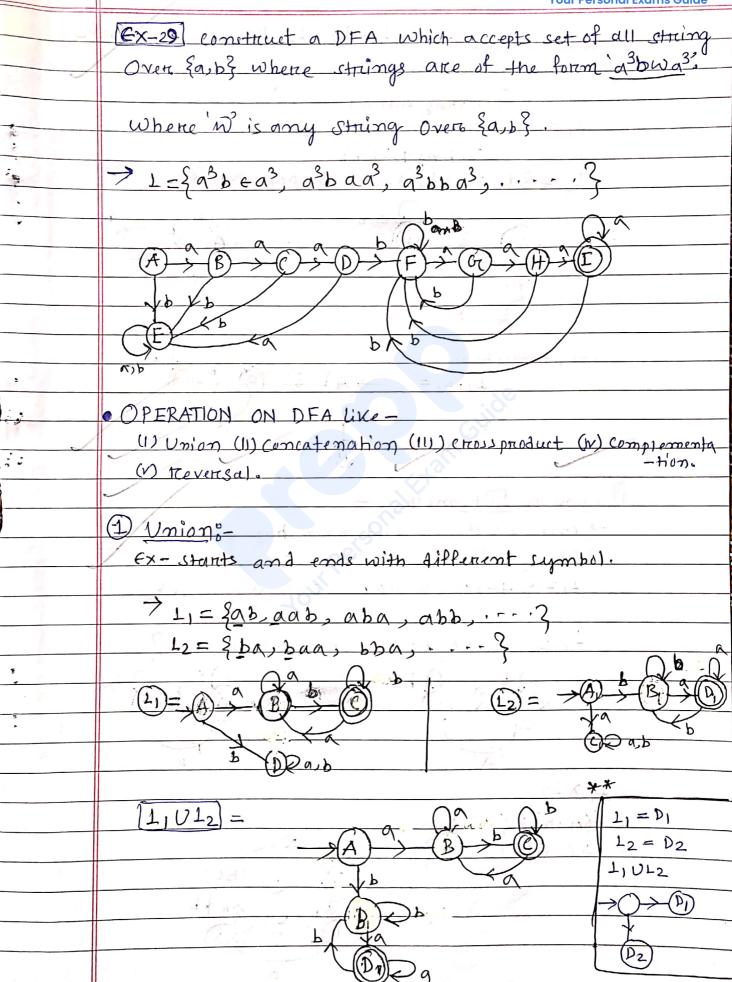


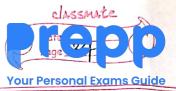
	Your Personal Exams Guide
	$[\epsilon \times -23]$
	Construct a minimal DFA which auepts, 1= {anbm/n,my1}
	Constitute of minimal DEA Which amples ("1")
	$\rightarrow 1 = \{ab, aab, aabb, aabb - \dots \}$
N.	
-	State transation diagram-
3.11	
	a Qa b
	B) + finial State.
	b to to
7.4	De a,b
	$[E_{X}-24]$
	Construct a minimal DFA, which accepts 1= {an, bm/nmho}
	2
	-> 1={E, a, aa, alla,, b, bb, bbb, ab, aabb}
0	Charle Atraneation Disconn
	State transation Diagram-
	QA. Qb. Apartice -
	$\rightarrow$ $(A)$ $\rightarrow$ $(B)$
Min-N	100 70
群 4	(C) a, b
1	[Ex-25]
	Constructs a minimal DFA, which accepts 1= {anhmcl/n,m,l,i}
	$\rightarrow 1 = \{abc, aabbcc \cdot \cdot \}$
	1 / 3 / / 12 / 12 / Come of the property of the state of the state of
	State transation diagram -
	a da b de com
	(B) $(C)$ $(D)$
	V DC La
	b, e (F) Pa, b, t
	1 1-1 3 A A A A A A A A A A A A A A A A A A

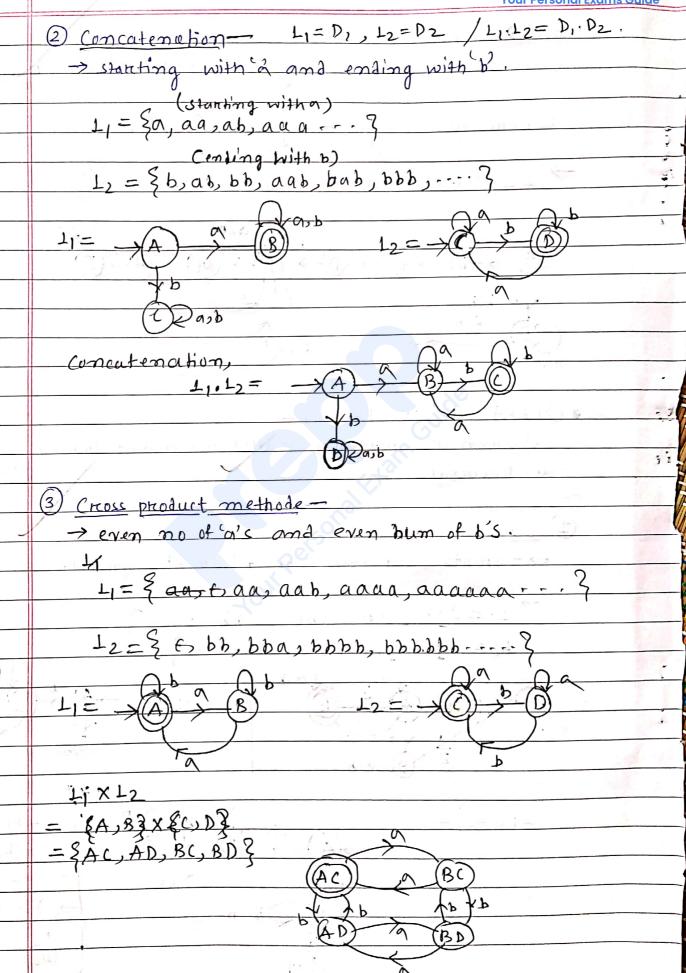






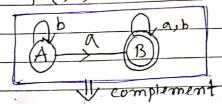


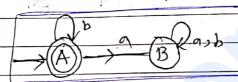




- 1) Complement: 
  > Does : Not Contain a.
  - 1)= { (ontaining a} = {a, aa, ab, ba, aaa...}

1,={e,b,bb,bb,bbb...}





(5) Reversal: → αWb (=> bWa.

 $L_1 = \{ \text{ ctant with } a_3 \}$   $= \{ a, na, ab, aaa, aba, aaaa \cdots \}$ 

$$I_1 = \{a, aa, ba, aaa, aba, aaaa \dots \}$$

 $L_{1} = A$  D = A

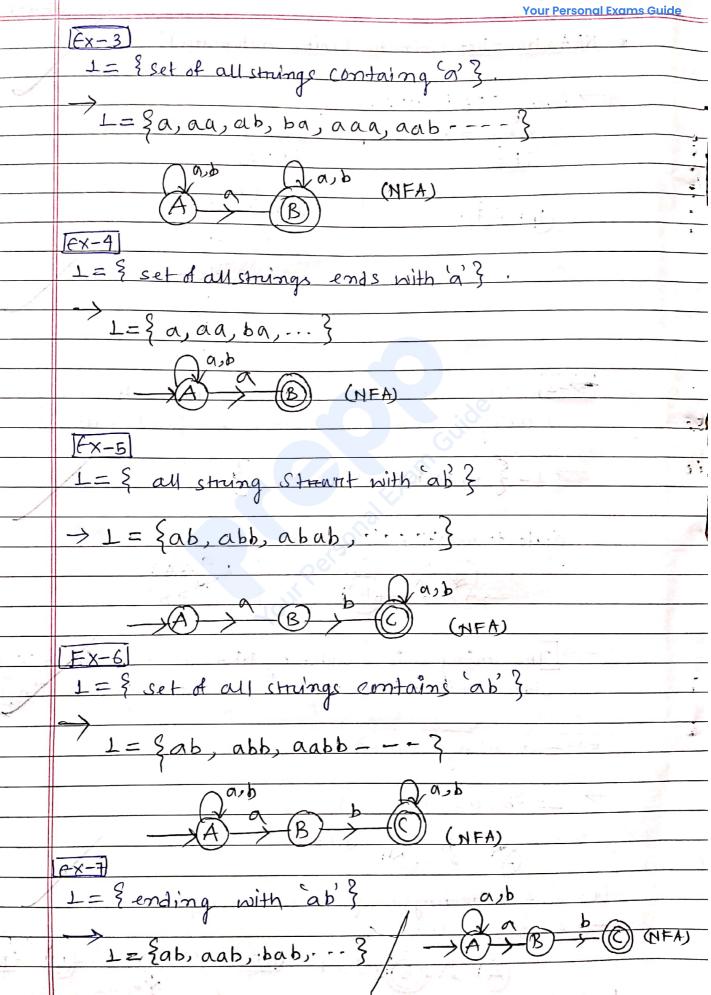
\*\*



	Your Personal Exan	ns Guide
	30 (Ex-30)	
	Construct a minimal DFA Over {a}.	7.3
~	1. Forc & an/m > 0, n! = 33	
	2. For { an/n>0, n!=2,n!=4}.	
	→ Z= \ a \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	
		,
		3
	$\perp = \xi e, \alpha, \alpha a, \alpha a a a, \dots$	
		đ
	$\rightarrow \bigcirc \bigcirc$	
		£
	(2) for $L = \{a^{m}/m / 0, n! = 2, n! = 4\}$	
	= 3 E, a, a a a, a a a a a, 3	ÿ <u>'</u> 2
	(A) (B) (C) (B) (E) (B)	164
	To the second of	
*		
*		
*		
	A 3 M 3 M 3 M 3 M 3 M 3 M 3 M 3 M 3 M 3	

d	> In NFA, not need to show death state.
The state of	NFA (Non-Deterministic Finite Automata):
	$\rightarrow$ $\vdash$ $\uparrow$
777	S: QXW > Q [S:QXW > 2Q]
	$\begin{array}{c c} S: Q \times W \rightarrow Q & S: Q \times W \rightarrow 2^{-1} \\ \hline DFA & NFA \end{array}$
	4 4 A C A 2 (1)
	$(90) \xrightarrow{\omega} (91)$ $(90) \xrightarrow{\omega} (91)$
	792
	193
4	794
	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
	17
	[22-1] Construct of NFA, wherewhich accepts cut of all
1	string over {a,b} such that 1 = {ends with a}
	$\rightarrow 1 = $ $\{ a, aa, ba, aaa, baa \dots \}$
	7 12 7 00,000, 5 7 DOLL
	State transation Diagram,
	B A B
- 1	
	-> [The string a' is accepted by NFA, if start with mitial
9	The string a' is accepted by NFA, If start with minal state and end if reach at least 1 state is final
- 5	
•	EX-2 1= {ending with b}
-	> L= {b, ab, abb}
	(A) (NFA)
	TEX-3] 1 = Stanting String Stants with a? }  \rightarrow L = \{\alpha, \alpha, ab \cdot \}
	A) A B (NFA) A B (DFA)
	A) B) a,b
	ababa Da,b







	CONVERSION of NEA to DEA for the Example 4 all
	Strings Start with a ". (1)
	<b>V</b>
	$\Rightarrow L = \{a, aa, ab, aab, abq, \dots, \}$
	State transation Diagram of NFA.
	man full the constraint and the
	a,b
	A) (B) (NFA)
	Marie Andrews in 19th Andrews
	STT of NFA-
	A B D I China
	X O D D
	· *BBB
	STT of DFA-
::	a b
	$\rightarrow A$ $B^{\sim}$ $D^{\sim}$
	*BBB
	D D D
30 · 4	
Ŧ	STD tof DFA-
:	$A \rightarrow B DDab$
Maria Service	
	Cocampia 3
	Exercision - 2
	Conversion of NFA to DFA:
)	LE ay strungs ends with a".
	-> { a, aa, abba, aaa, aba, }
1	, conjugación de la conjugació
201 7 24 7 7	, ⊗ ji™



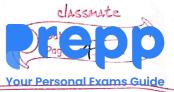
	Your Perso	nal Exams Guide
ST-Dia	igham of NFA- ST-table of NFA	V.
	1 a b	
	A {A,B} {A}	
	(A) B {0} 50}	
ST-TO	uble of DFA ST-Diagram of DFA	The state of
	3 Viagion V	1
	a b Qa	
→A	[AB] $[A]$ $(AB)$	
		11
* [AB	(AB) (A)	2 3
		]-
€x_2		4
	version of NFA to DFA,	
1= 8	au chrings in which third symbol from	8. H. C. C. S.
		٠٠٠٠ الله
$\rightarrow$ 1	= {aaa, abb, aba, baaa,}	
1-72	of NFA	
	asb	
		Į.
(A	$(B) \rightarrow (B) \rightarrow (D)$	
	<u> </u>	
ST	Table of NFA	
	and the second second	1
	a ba	
$\rightarrow$ /	A {A,B}	27 12 1 2 2
	B {c} {c}	197
	C { \$ p3	Lower 1
*	D 803 803	
	The state of the s	Late walls
		3 m 1 m 1 m 1 m 1 m 1 m 1 m 1 m 1 m 1 m



				Your Person Mickards Suide
	ST-Tabl	e of DFA A	пот <b>s</b> -тт	of NFA-
	1	a _	Ь	
	> [A]	[A,B)'	[A]Y	D C C C C C C C C C C C C C C C C C C C
	[AB]	[A,B'c]^	TAC)	
	(AC)	[ABD)	[AD]	
	*[AD]	(AB)	[A]'	(
_	(ABC)	[ABCD]	[ALD]	·
	*[ABD]	[ABCY	[AC]'	33
	*(ACD)	(ABD)	[AP]'	
)s	*[ABCD]	[ABCD]^	[ALD]	
	0 - 0	0		
100	ST-Diag	tram of DF	A from a	above STT of DFA-
7.1	Ob	(AB)	19	ABC BB
	-\A\	7	KI	b (ACD)
-		Y b	b AD	
	Ь	(AC)	-09/	(ABD)
	1.	<b>\rightarrow</b>		
	(ATA)	11		
1.1	ees 1	1 12-3	A	BCD
	and marked			<b>不</b>

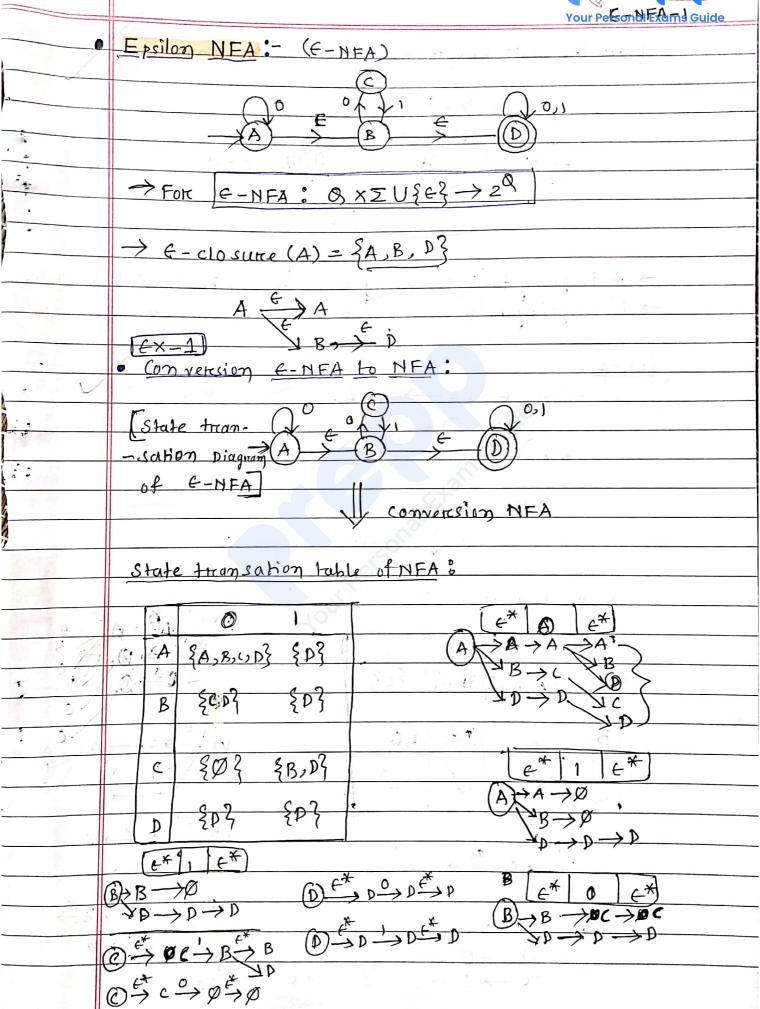
If an minimal NFA Contain n' states then an DFA Contain 2<sup>n</sup> states in worst case.

n -> 2<sup>n</sup>



	Your Personal Exams Guide
	JEX-) NFA for Gring of length-
	a) exactly 2. b) at most 2 c) at least 2
	$(b) \rightarrow L = \{\epsilon, \alpha, b, \alpha\alpha, ab, b\alpha, bb\}$
-	A) 00 B) 0
	Tanak Lasting Tanak Lasting
	$C \rightarrow L = \{ aas abs ba, bb, aaa, \}$ $A \rightarrow B \rightarrow C$
	**
	It is going to be no States.
	· COMPLEMENTATION of NFA
	$\Sigma = \{\alpha, b\}$ $I \neq I $ (In NFA)
	1 = { starts with a } oB-11 what is the language accepted by the Comprement of NEA.
	$L_1 = \{a, ab, ab, \dots, 3\} \rightarrow \{e\}$
(\$ -	of ranguage accepted by NFA.
	There $A$



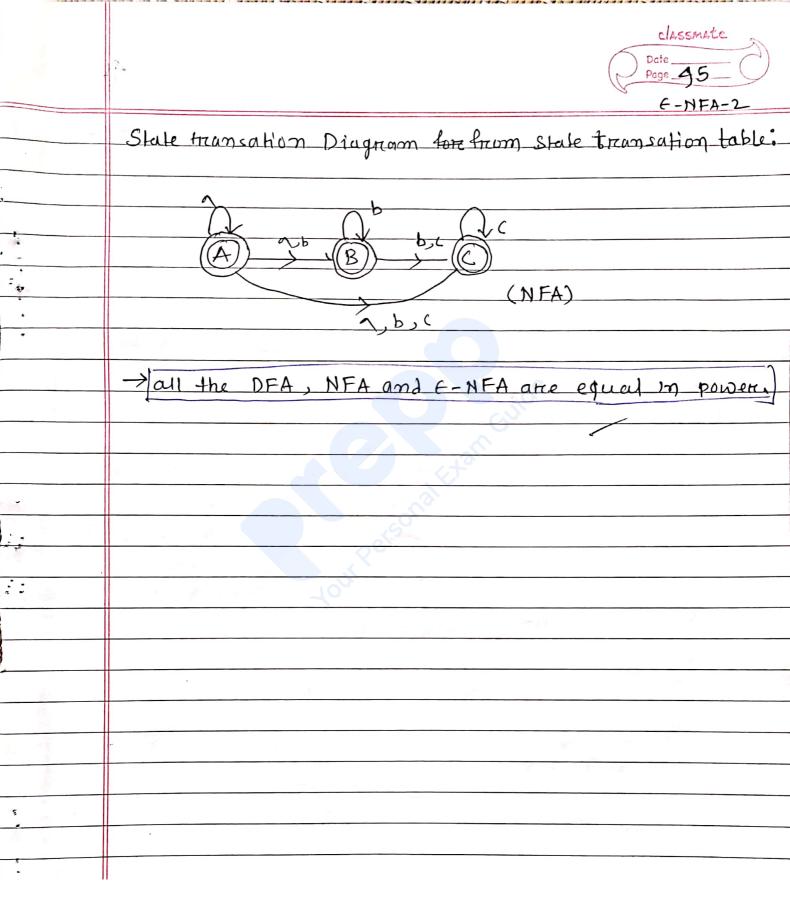


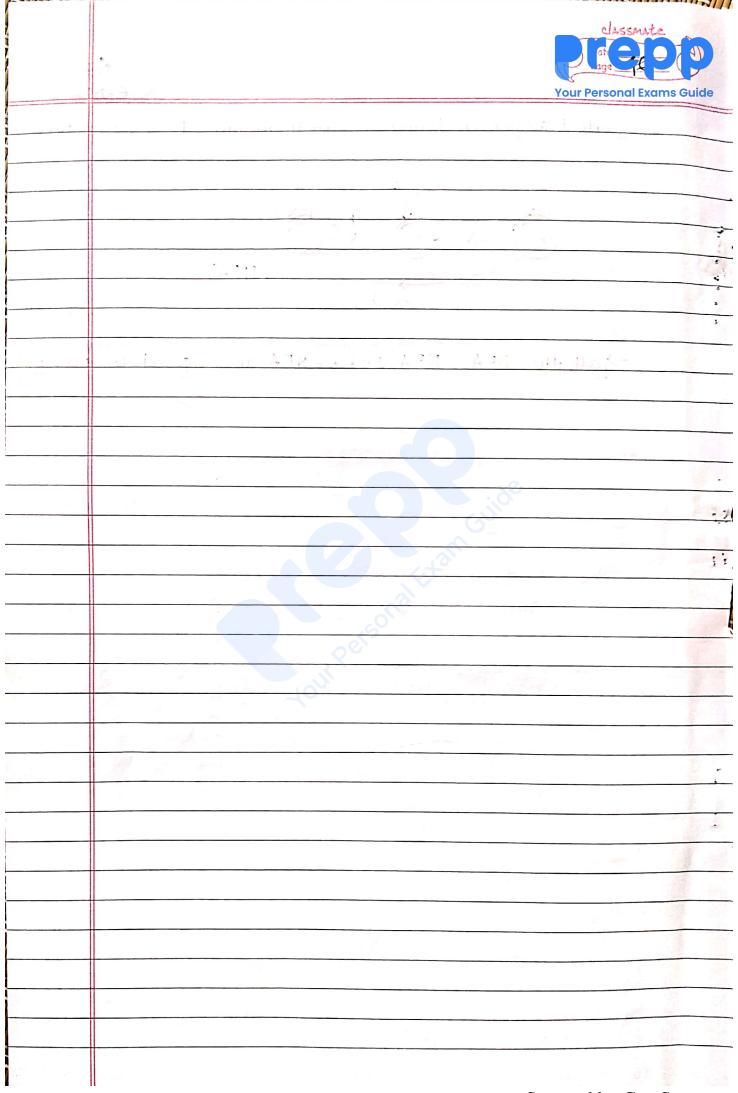
4

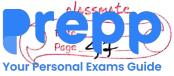


	Your Personal Exams Guide
	from the state table trom sation Diagram - we
	0 C 10 0 0 0,1
	$\rightarrow (A) \rightarrow (B) \rightarrow (D) \geq 0$
	70
	→ 'A' is going to 'D' by seeing E' so A' will be the finiou state.  → 'B' is going to 'D' " " " E' so, B' " " ".
	$\boxed{(+\times-2)}$
0	conversion ENFA -> NFA.
	A B B C C
	(CHFA)
	1 conversion.
	trunsation table:-  A $\xi_A$ , $g$





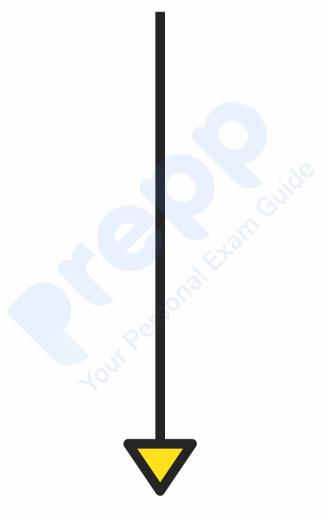




				Your Personal Exams Guide		
0	Minimisation of DFA:	f d	1.	į.		
	**	1 . 6	. 6	0 ←		
1	Two State called equi	valent,				
-	(B9) equivalent		10	β		
	S(PW) EF					
	=> S (9,W) EF	- P	A, p	P		
J.	ОП	- N 2	. 6	β		
	S (P,W) & F	9-	12	, p s		
	⇒ d (9, w) # F		F 2			
	When			,		
1	length of string I is	0 = 0	O en wive	alkooth (A)		
1	1 in	)]=1	1 Paul			
	Tim	1=2	2 equi.			
	}					
l C	34124	N <sub>1</sub> that	0	s Amila (2)		
	[w]=n, n equivalent.					
	Example - 1	196	P . P . o [	7		
V	Minimise the given DF	A -				
	90	L III NA	"e" ma	(B) Fright		
	$\alpha \stackrel{(q_1)}{\longrightarrow} \frac{(q_3)}{}$					
	40		PL (sp.			
	A Ta	<b>Y</b> b	1=0			
	b a	(4)	S tun	bind (b)		
		5	1 2 1/3	5111		
	Larger Cr. P. C. P. S. P. P. P. S. P. P. P. S. P. P. P					
	-> Step-1: Identify the Initial state and final state.					
	o transity)	- ( ( -	1 STUTE OF	nd timal state.		
	Cten - 2 ° Dal-to VII	الداء ما	11 . 1	in fina		
Mr. Ar	Step-2 : Delete all	The Stat	e that	not reachables		
	from initia	1 State	7	-		
	Step-3: Draw Sta		4	•		



## CLICK ON THE LINK GIVEN BELOW



**WWW.GATENOES.IN** 

**GATE CSE NOTES**